

# Performance of a solid-state frequency-shifted feedback laser in optical ranging

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The performance of a frequency-shifted feedback laser (FSFL) using a Nd:YVO<sub>4</sub> crystal as gain medium was investigated as light source in high accuracy optical ranging based on optical-frequency domain reflectometry (OFDR). The FSFL generates a comb of chirped frequency components over a bandwidth of 45 GHz with chirp rates of  $3.8 \times 10^{17}$  Hz/s. In OFDR, distance accuracies better than 25  $\mu\text{m}$  at a data measurement time of 2 ms were demonstrated at a standoff distance of 5 m. The results show that the FSFL is a promising light source for high accuracy, high speed 3D measurement applications. [DOI: 10.2971/jeos.2009.09010]

**Keywords:** frequency-shifted feedback laser, solid-state laser, optical ranging, distance measurement

## 1 INTRODUCTION

A frequency-shifted feedback laser (FSFL) has a frequency shifter in its cavity such that the intracavity field is frequency shifted by a fixed amount at every round trip. As a consequence, this laser behaves differently from a conventional laser. In the continuous wave regime, an FSFL can generate a comb of chirped frequency components with very high chirp rates, over a broad bandwidth [1]–[4]. Such a light source is of great interest for high accuracy, high resolution ranging applications based on optical frequency-domain reflectometry (OFDR). These applications include remote sensing, fiber characteristics measurements in telecommunications, 3 dimensional (3D) shape measurements for quality inspection in industry, structural health monitoring.

The great potential of the FSFL as light source for these applications has motivated the study of numerous cavity configurations incorporating various gain media. Previously, FSFLs operating in the 1550 nm window using erbium-doped fibers [5] or semiconductor optical amplifiers [6] have been widely studied for their potential as light source in high accuracy optical ranging. Owing to their short cavity lengths, solid-state FSFLs operating at 1  $\mu\text{m}$  offer the possibility of generating a chirped comb with faster chirp rate than their fiber counterparts. Furthermore, by using these lasers as pump light source, FSFL operation in the green portion of the spectrum by second harmonic generation is of interest to achieve higher spatial resolution, higher distance accuracy. The spectral characteristics of the Nd:YVO<sub>4</sub> FSFL and its ability for long distance ranging has been extensively studied for ranging previously [7]; however, as with other FSFL, there remains some work to do on investigating the performance in long range, high accuracy ranging applications, namely 3D shape measurements.

## 2 FREQUENCY-SHIFTED FEEDBACK LASER

A schematic of the solid-state FSFL we used in these experiments is shown in Figure 1. The gain medium was a 1 mm Nd:YVO<sub>4</sub> crystal and was pumped by a fiber pigtailed laser diode (Lumics) generating an output of 3 W at 808 nm. The 1064 nm beam was collimated using a 40 mm lens. The cavity was formed between a highly reflective mirror and an output coupler mirror having a reflectivity of 80%. The frequency shifter was an acousto-optic modulator (AA Optoelectronics) generating a round trip frequency shift of 280 MHz. The modulator had a maximum diffraction efficiency of 80% with 1 W of RF input power. The cavity length was about 10 cm.

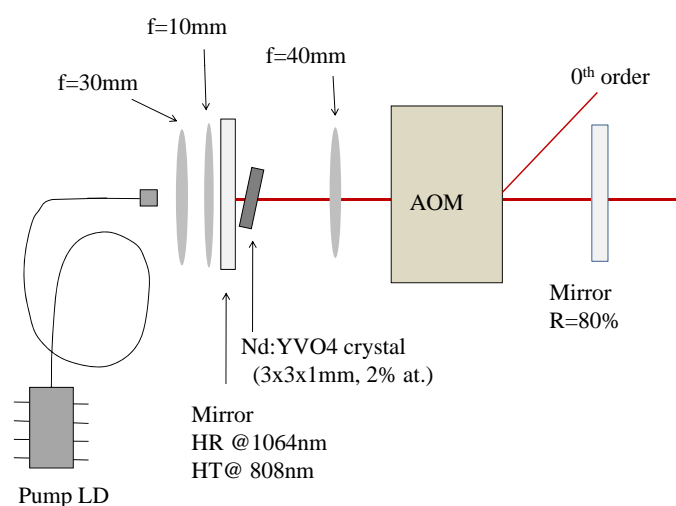


FIG. 1 Schematic of the Nd:YVO<sub>4</sub> FSFL.

Oscillation threshold of the FSFL was about 50 mW, the slope efficiency was 15%. Observations of the laser intensity using a digital oscilloscope showed that the FSFL tends to operate in the pulse regime at high pumping power (beyond 1W). For the interferometric experiments described below, the laser was operated at moderate pumping powers, avoiding the pulse regime.

### 3 PERFORMANCE OF THE FSFL IN RANGING

#### 3.1 Optical spectral characteristics

Figure 2 shows an optical spectrum of the FSFL centered at 1064.27 nm. For high accuracy optical ranging using an FSFL, a broad bandwidth is mostly desired as indicated in the next section. The laser spectral profile was affected by many factors such as the gain profile, spectral filtering caused by some residual reflections from the output coupler or laser crystal facets. With adjustments of the pumping power or frequency shift, the FSFL optical spectrum was at times as broad as 60 GHz, however spectral distortions appear after some time, due to some instabilities. For more stable and accurate measurements, a stable and uniform spectrum is desirable. The laser parameters were adjusted to obtain a smooth spectrum with the broadest full width at half maximum (FWHM) of 0.18 nm ( $\sim 48$  GHz). It is worth noting that these results show a significant improvement from earlier studies FSFL using Nd:YVO<sub>4</sub> in which the spectral widths were in the range of 10 GHz [3]. We found that minimizing the residual reflections was of great importance in achieving broad bandwidths.

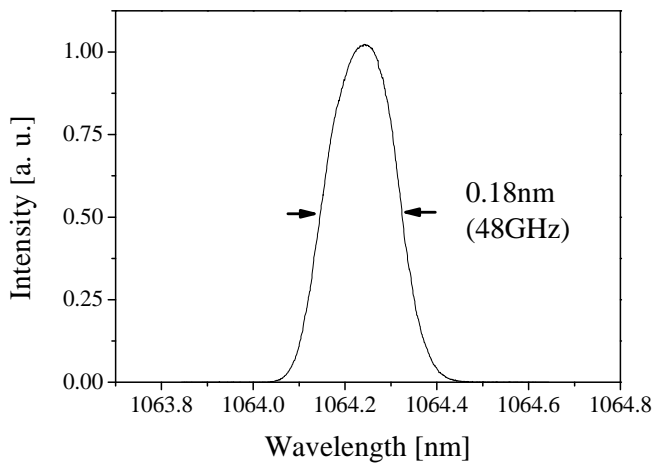


FIG. 2 Optical spectrum of the Nd:YVO<sub>4</sub> FSFL.

#### 3.2 OFDR with the FSFL

A schematic of the OFDR setup using the FSFL as light source is shown in Figure 3. The FSFL output was collected with a collimator and split with a 1/99 fiber coupler. A small amount was taken as reference using a 3 dB coupler, while the bulk of the output ( $\sim 40$  mW) was focused to a beam diameter of about 2 mm onto an aluminum plate placed at 5 m, then the scattered light was sent to the 3 dB coupler via an optical circulator. All the fiber components were polarization maintained. The interferometer output was analyzed using either

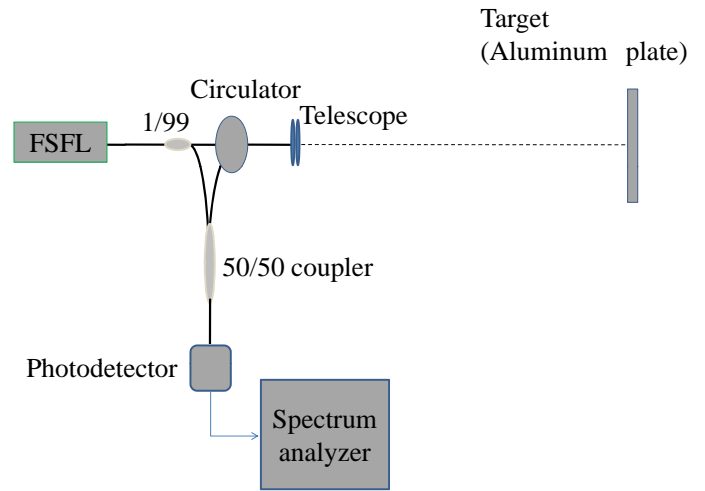


FIG. 3 Setup of the OFDR system.

a real-time or radio frequency (RF) spectrum analyzer after photodetection (Newfocus 1611).

Figure 4 shows the RF spectrum of the interferometer output observed with the RF spectral analyzer. It shows a beat signal at the cavity free-spectral range (FSR = 1.35 GHz), corresponding to a cavity length of 11 cm. The beat signals A and B were generated from interference between the delayed components of the chirped comb. The beats A were generated from the target, while those shown in B were from spurious reflections at the fiber end in the telescope. These interferometric beat signals can be expressed as [7]

$$\nu_{Bm} = \nu_s \nu_c \frac{2z}{c} - m\nu_c \quad (1)$$

$$m = \nu_s \nu_c \frac{\Delta \nu_{Bm}}{\Delta \nu_s} - \nu_c \nu_{Bm} \quad (2)$$

Here  $\nu_{Bm}$  is the beat frequency,  $\nu_s$  is the frequency shift,  $\nu_c$  is the FSR,  $z$  is optical path length,  $c$  is speed of light,  $\Delta \nu_{Bm}$  is the beat frequency variation when the frequency shift changes by  $\Delta \nu_s$ ,  $m$  is an integer representing the beat order. The distance is given by :

$$z = \frac{c}{2\nu_s \nu_c} (\nu_{Bm} + m\nu_c) \quad (3)$$

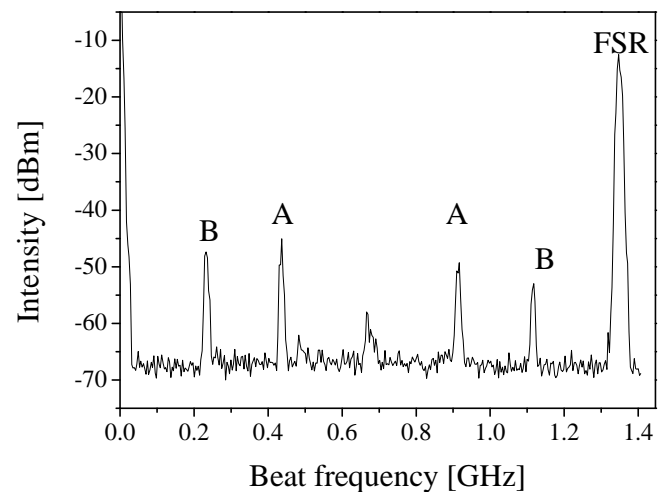


FIG. 4 RF spectrum of the interferometer output. Resolution was 1 MHz.

Figure 5 shows the RF spectrum of one interferometric beat signal measured using the real-time spectrum analyzer. The resolution of the analyzer was 100 KHz and the data were averaged 10 times. The measured beat bandwidth was approximately 8 MHz. If the FSFL spectral components chirp throughout the laser bandwidth  $\Delta\nu$ , at the rate  $\nu_s\nu_c$ , then after a Fourier transform at the spectrum analyzer, the beat bandwidth is approximately as  $\nu_s\nu_c/\Delta\nu$ . From the measured parameters, the calculated beat bandwidth is 7.8 MHz. Therefore we can state that the spectral components chirp continuously across the chirp range  $\Delta\nu$ , without phase discontinuity. The distance resolution  $\delta z = c/2\Delta\nu$  is then approximately 3 mm in this case.

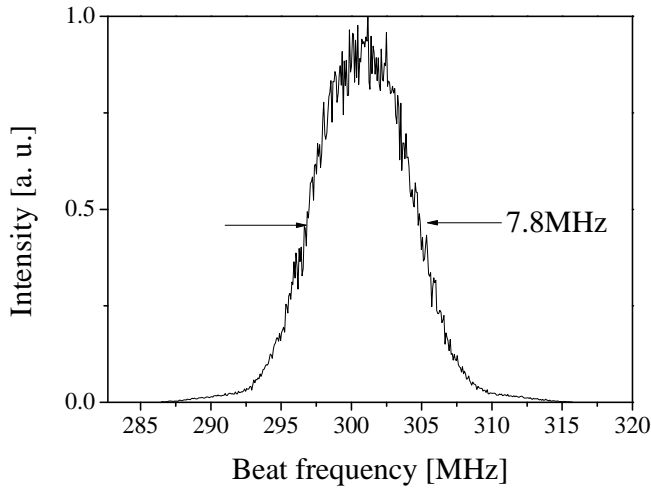


FIG. 5 RF spectrum of an interferometric beat signal after 10 averaging. Resolution was 100 KHz.

### 3.3 Distance accuracy in FSFL ranging

The distance accuracy is related to the uncertainty in determining the center frequency of the beat signal. Using Eq. (3), the uncertainty on the distance can be written as

$$\begin{aligned}\sigma^2(z) &= \frac{c^2}{4} \sigma \left( \frac{\nu_{Bm}}{\nu_c \nu_s} + \frac{m}{\nu_s} \right)^2 \\ \sigma^2(z) &= \frac{c^2}{4} \left\{ \left( \frac{\sigma(\nu_{Bm})}{\nu_c \nu_s} \right)^2 + \frac{\nu_{Bm}^2}{\nu_c^2 \nu_s^2} \left( \frac{\sigma^2(\nu_c)}{\nu_c^2} + \frac{\sigma^2(\nu_s)}{\nu_s^2} \right) \right. \\ &\quad \left. + \left( \frac{\sigma(m)}{\nu_s} \right)^2 + m^2 \left( \frac{\sigma(\nu_s)}{\nu_s^2} \right)^2 \right\}\end{aligned}\quad (4)$$

neglecting the uncertainty on  $m$ , this expression can be further simplified to

$$\sigma^2(z) = \frac{c^2}{4} \left( \frac{\sigma(\nu_{Bm})}{\nu_c \nu_s} \right)^2 + \frac{c^2}{4} \frac{\nu_{Bm}^2}{\nu_c^2 \nu_s^2} \left( \frac{\sigma^2(\nu_c)}{\nu_c^2} + \frac{\sigma^2(\nu_s)}{\nu_s^2} \right)^2 \quad (5)$$

The uncertainty on the beat frequency  $\sigma(\nu_{Bm})$  depends essentially on the beat bandwidth as well as the frequency resolution of the frequency measurement (spectrum analyzer in our case). This uncertainty can be expressed as [8]

$$\sigma(\nu_{Bm}) \approx \sqrt{\Gamma/T_0}, \quad (6)$$

where  $\Gamma = \nu_s\nu_c/\Delta\nu$  is the beat bandwidth and  $T_0$  is the measurement time of the beat signal. Inserting this to Eq. (6), a

general expression for the uncertainty in the distance is

$$\begin{aligned}\sigma^2(z) &\approx c^2 \left( \frac{1}{4\nu_c \nu_s \Delta\nu T_0} \right) + c^2 \frac{\nu_{Bm}^2}{4\nu_c^2 \nu_s^2} \left( \frac{\sigma^2(\nu_c)}{\nu_c^2} \right) \\ &\quad + z^2 \left( \frac{\sigma(\nu_s)}{\nu_s} \right)^2.\end{aligned}\quad (7)$$

The term  $\sigma(\nu_s)/\nu_s$  depends on the stability of the RF source used to drive the AOM. For stability levels of  $10^{-7}$  or better, the distance does not significantly affect the accuracy for few tens of metres. Also by having the laser cavity stable enough, at distances of few meters, the distance accuracy can be expressed as

$$\sigma(z) \approx \frac{c}{2\sqrt{\nu_c \nu_s \Delta\nu T_0}}. \quad (8)$$

To verify this result, we measured the distance accuracy at a standoff distance of 5 m in the laboratory environment. The peak frequency of the beat shown in Figure 5 was measured for 128 data points. The measurement time (time for Fourier Transform) for a single point was set at 2 ms. Figure 6 is a plot of the distance accuracy as a function of data averaging time. For a measurement time of 2 ms, the calculated accuracy using the laser parameter was  $25 \mu\text{m}$ , which is in good agreement with the measured results. In 3D shape measurement in which we are more interested, this result corresponds to a distance accuracy of about  $35 \mu\text{m}$  for a measurement time of 1 ms or measurement speed of 1000 points/second. In these experiments the laps between data acquisition was long due to our spectrum analyzer and the program to acquire the data. Therefore at very long data averaging times, cavity instabilities become important and the distance accuracy is dominated by the second term of Eq. (8), reaching a limit at few micrometres. We believe that faster data acquisition and longer averaging could possibly lead to submicrometer accuracy at few seconds.

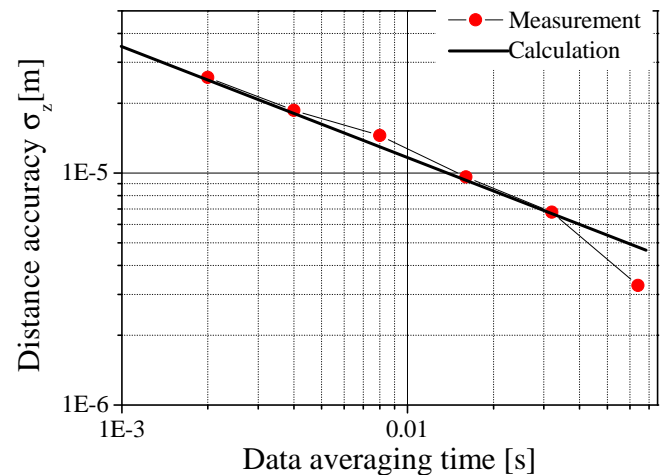


FIG. 6 Distance accuracy as a function of data averaging time.

As a demonstration of the system, small displacements were measured by moving the target by  $50 \mu\text{m}$  steps. 50 data points were measured with a single data point measurement time of 2 ms. The relative distance variation is shown in Figure 7. By independently measuring the deviation from these data, the distance accuracy was  $25 \mu\text{m}$ , which is in good agreement with the result previously obtained in Figure 6.

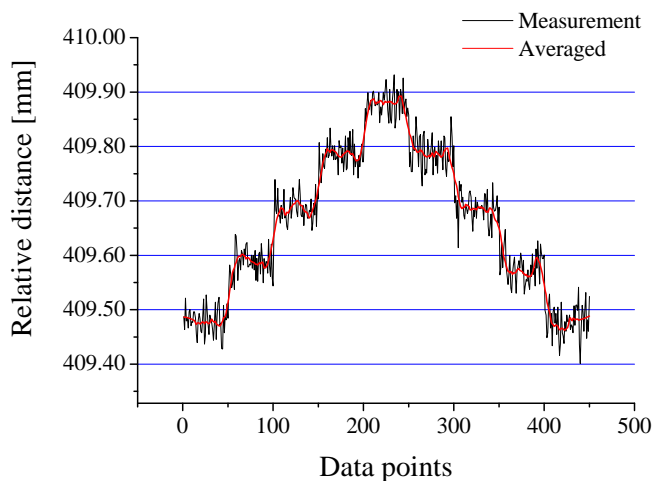


FIG. 7 Measurement of small displacements.

In summary a frequency-shifted feedback laser using a Nd:YVO<sub>4</sub> crystal as gain medium was investigated as light source in high accuracy optical ranging based on optical-frequency domain reflectometry. Chirped comb generation over a bandwidth broader than 45 GHz with chirp rates of  $3.8 \times 10^{17}$  Hz/s has been obtained. The performance of this laser in optical ranging was investigated and distance accuracies better than  $25 \mu\text{m}$  for measurement times of 2 ms were demonstrated, corresponding to measurement speeds of 500 points per second or  $35 \mu\text{m}$  at 1000 points/s. These results show the highpotentiality of the FSFL as light source for high

accuracy and high speed 3D measurement applications.

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